Std IX

# MAR THOMA RESIDENTIAL SCHOOL, TIRUVALLA ANNUAL EXAMINATION 2017 - '18

MATHEMATICS
Section A ( Answer all questions )

Marks:: 80 Time: 2½ hrs

# Question 1

(a) Calculate the rate of interest if \$8000 amounts to \$10648 in 3 years at compound interest [3]

(b) Solve: 
$$7(y+3)-2(x+2) = 14$$
,  $4(y-2)-3(x-3) = 2$ , simultaneous equations. [4]

(c) Evaluate 
$$\frac{\sin 77}{\cos 13} + \sin^2 42 - \cos^2 48 - 3 \tan^2 45$$

[3]

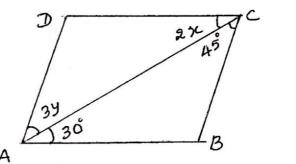
#### Question 2

(a) If 
$$(a + \frac{1}{2})^2 = 5$$
 then show that  $a^3 + \underline{1} = 2\sqrt{5}$ 

(b) A cuboid has its edges in the ratio 1:2:7. If the volume of the cuboid is 378 cm<sup>3</sup>, find its total surface area.

[4]

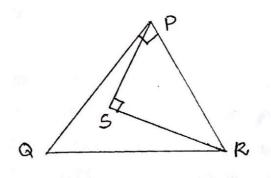
(c) In the figure ABCD is a parallelogram. Find the Values of x & y.



[3]

#### Question 3

(a) In  $\triangle$  PQR,< QPR = 90° and QR = 26 cm. If PS  $\triangle$  SR, PS = 6 cm and SR = 8 cm. Find the area of  $\triangle$ PQR



[3]

(b) Factorise (i) 
$$x^2 - 30x + 216$$
 (ii)  $3x^4 - 243$ 

[4]

(c) Evaluate 
$$\log 81 - 2 \log 3 + 3 \log 2 + \log 3$$
  
8 2 3 4

[3]

#### Question 4

(a) Simplify  $2^{10+a} \times 4^{3a-5}$  [3]  $2^{4a+1} \times 2^{3a-1}$ 

(b) A boy has pens and pencils which are together 40 in numbers. If he had 5 more pens and

5 less pencils, the number of pens become four times the number of pencils. Find the original number of each.

[4]

(c) If A is an acute angle and cosec A =  $\sqrt{2}$ , find the value of  $3 \sin^2 A + 3 \cot^2 A$ 

$$tan^2 A - cos^2 A$$

[3]

# Section $oldsymbol{B}$ (Answer any 4 questions only )

#### Question 5

- (a) Solve for x,  $\log (10 x + 5) \log (x 4) = 2$
- (b) ABCD is a rectangle with AB = 48 cm. M and N are the midpoints of its sides BC and CDrespectively. If MN = 25cm, Calculate (i) the area of the rectangle ABCD
- (ii) The area of the Δ MCN.
- (c) Rohit borrows Rs. 86000 from Arun for 2 years at 5% p.a simple interest. He immediatel lends out this money to Akshay at 5 % compound interest compounded annually for the same period. Calculate Rohit's gain in the transaction at the end of 2 years.

#### Question 6

- (a)  $16^{3/4} \times 25^{-3/2} \cdot 5^{-3}$ 81 9 2
- (b) If A (p, q) is equidistant from P (-4, 3) and Q (3, -4) Show that p = q
- (c) In a  $\triangle$  ABC,  $2(A-20^{\circ}) = (B+10^{\circ}) = 2(C-10^{\circ})$ . Find each angle of the triangle.

#### Question 7

- (a) Construct a parallelogram whose diagonals are 4 cm and 5.8 cm. The angle between the diagonals is 60°.
- (b) Factorise
- (i)  $a^3 + b^3 + a + b$  (ii)  $16x^2 y^2 + 4yz 4z^2$

### Question 8

- (a) Solve 5x y = 5 and 3x y = 3 graphically. Determine the co-ordinate of the vertices of the triangle formed by these lines and the y-axis.
- (b) ABCD is a parallelogram of area 900 cm<sup>2</sup>. AP is drawn perpendicular to BC and AQ is drawn perpendicular to DC. If AP = 24 cm and AQ = 18.75 cm, Calculate (i) AB (ii) BC and (iii) area of ΔABC.

#### Question 9

- (a) Simplify  $9^{3/2} 3(5)^0 (\frac{1}{81})^{-1}$
- (b) If a+b-c=4 and  $a^2+b^2+c^2=38$ , Find ab-bc-ca
- (c) Each of equal sides of an isosceles triangle is 4 cm greater than its height. If the base of the triangle is 24 cm; Calculate the perimeter and the area of the triangle

# Question 10

- (a) Show that the points A(1,1), B(4,1), c(4,4) and D (1,4) are the vertices of a square
- [3]

- (b) If a + b = 9 and ab = -2,
- Find:
- (i) a b
- (ii)  $a^2 b^2$

[3]

(c) In the given figure AB = AC,

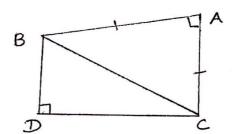
<A =< D = 90°, BD = 18 cm and

DC = 24 cm. Calculate the length

of AB correct to two places of

decimal. Also, find the perimeter

of quadrilateral ABDC



[4]

# Question 11

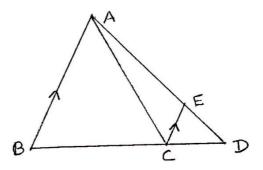
(a) Calculate the compound interest accrued on ₹16,000 in 3 years, when the rates of interest for successive years are 10 %, 12 % and 15 % respectively

[3]

(b) If  $\sin A = \underline{12}$  Evaluate  $\underline{1}$  tan<sup>2</sup> A  $\cos^2 A$ 

[3]

(c) In the figure AB = BC, CE is parallel to BA, < ACD = 103° and < AEC = 52°. Prove that CE = ED



[4